

# SCALE VARIATIONS AS THEORETICAL UNCERTAINTIES

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*Simone Devoto*



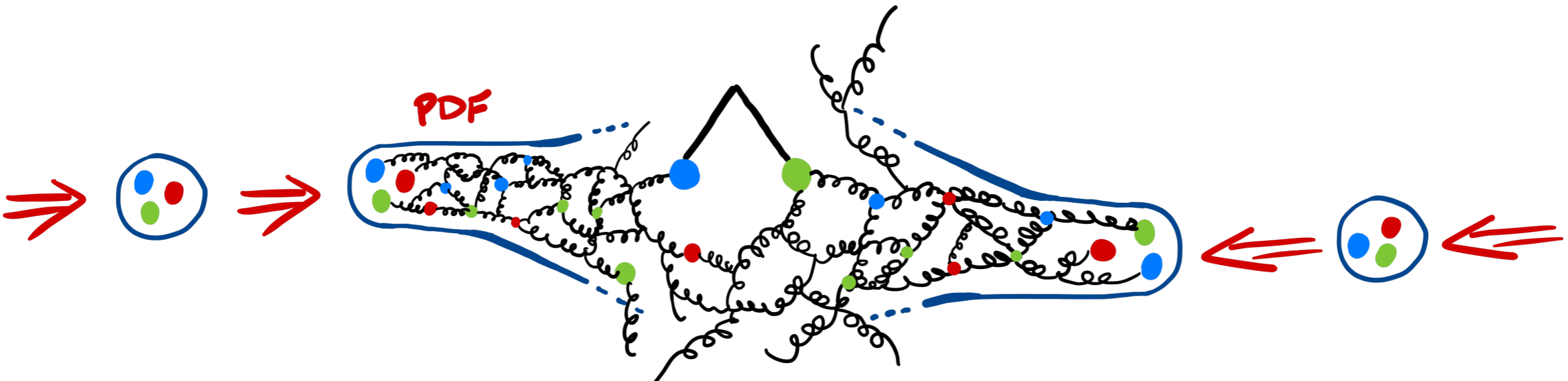
GHENT  
UNIVERSITY



FACULTY  
OF SCIENCES

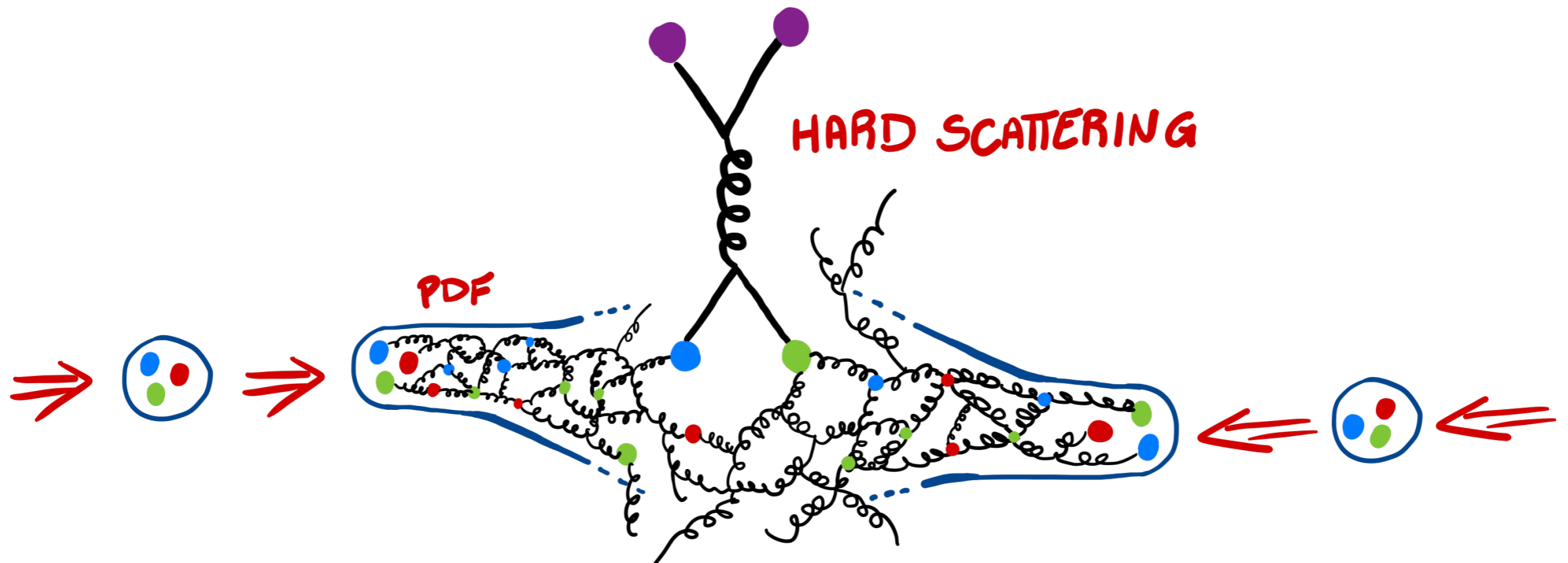
# THEORETICAL INGREDIENTS

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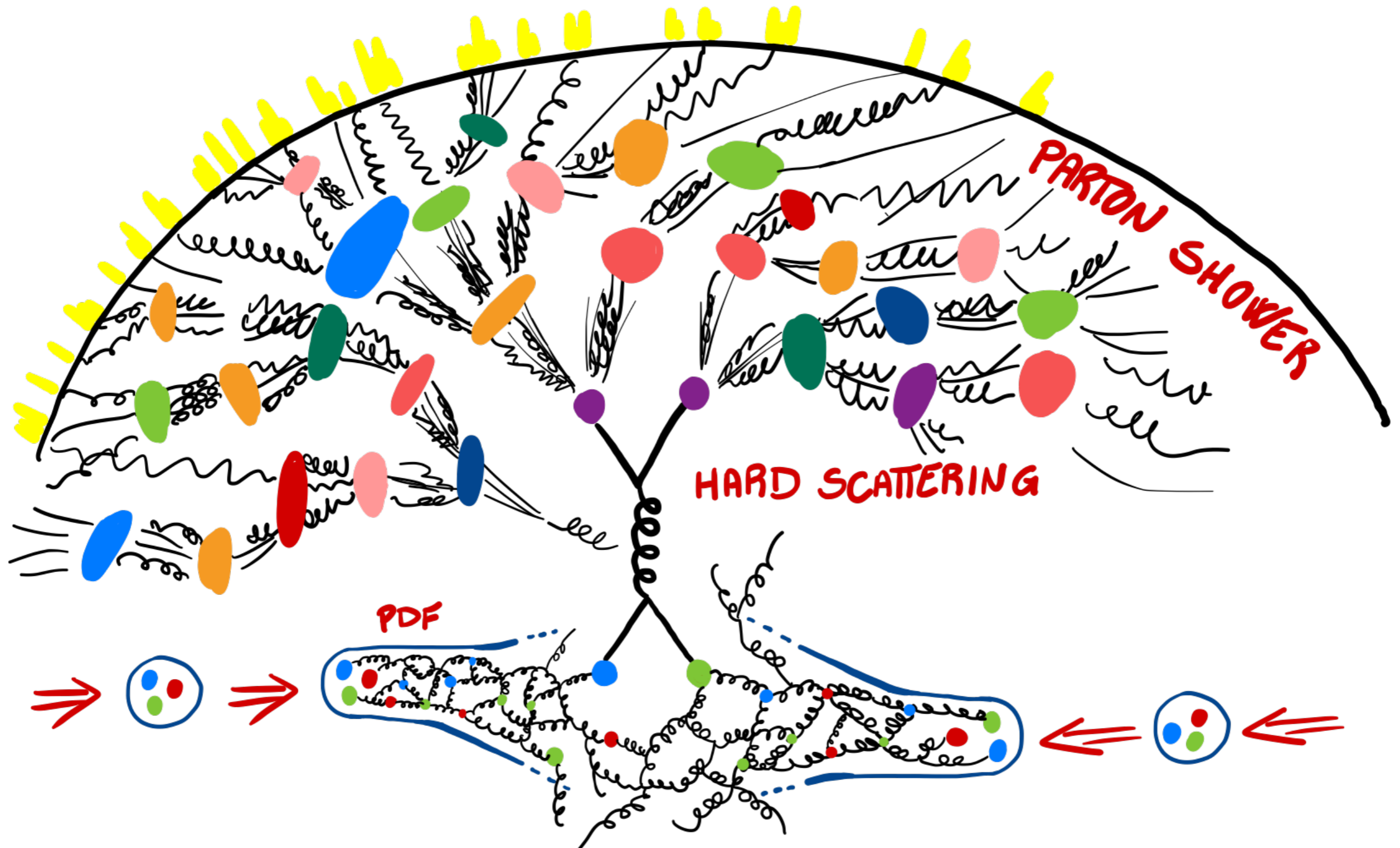
# THEORETICAL INGREDIENTS

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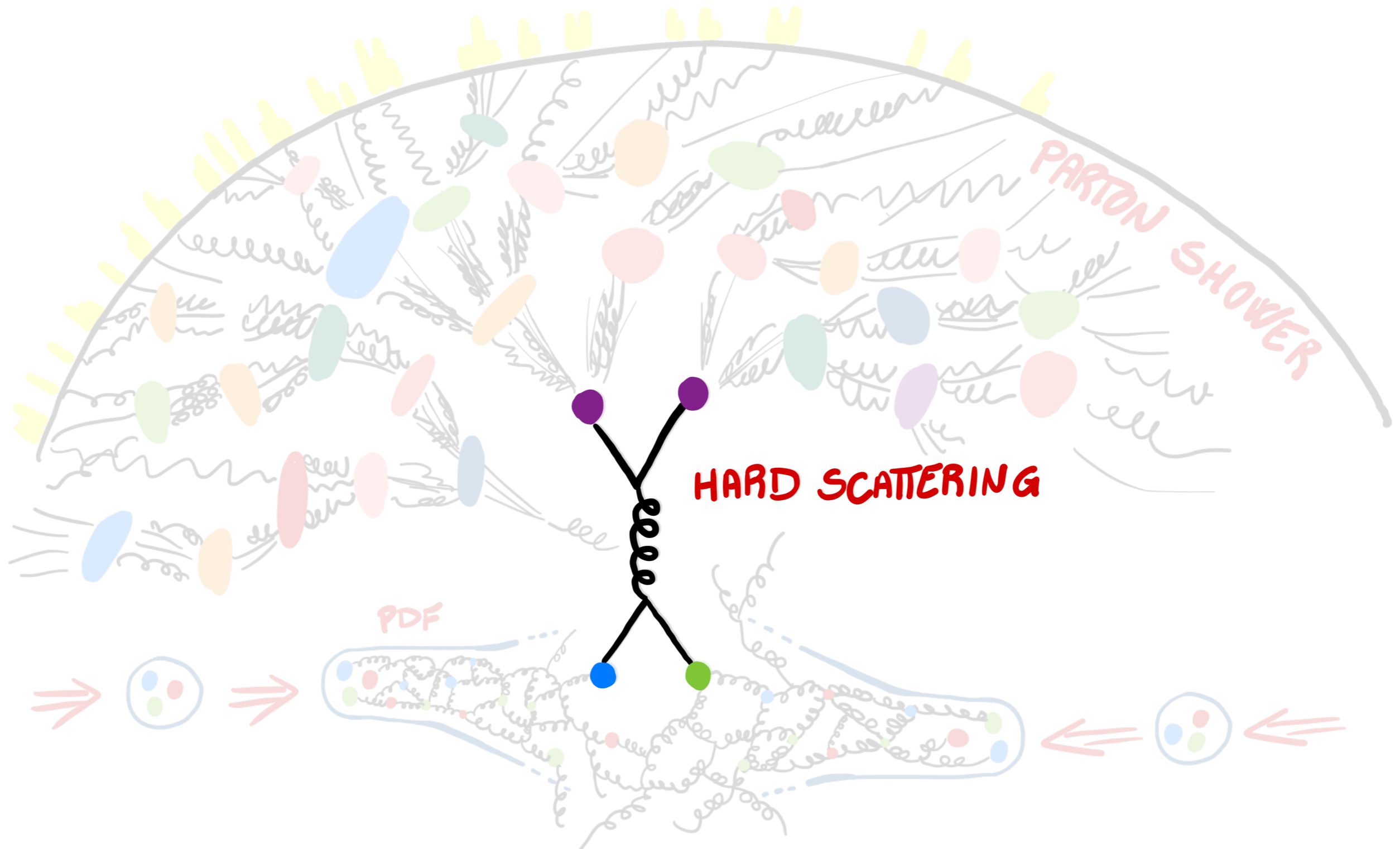
# THEORETICAL INGREDIENTS

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# THEORETICAL INGREDIENTS

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# PRECISION TESTS OF THE STANDARD MODEL

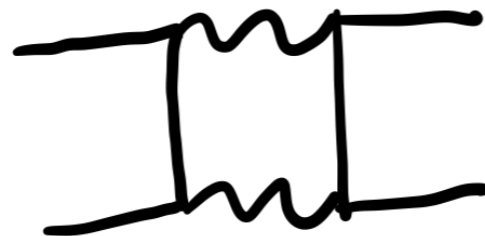
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- High precision in the theoretical prediction requires the computation of **higher order corrections**.

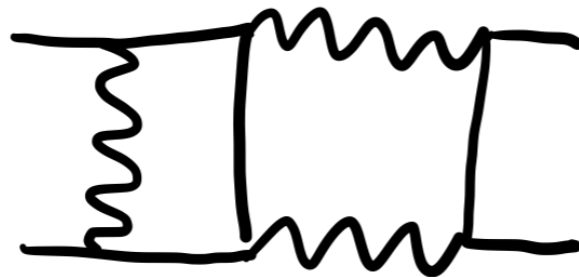
LEADING  
ORDER (LO)



NEXT-TO  
LEADING  
ORDER (NLO)




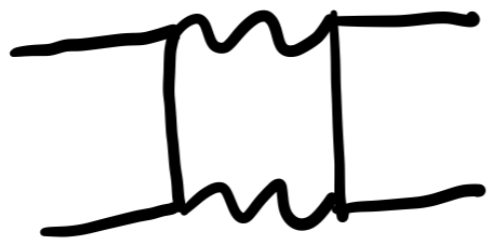

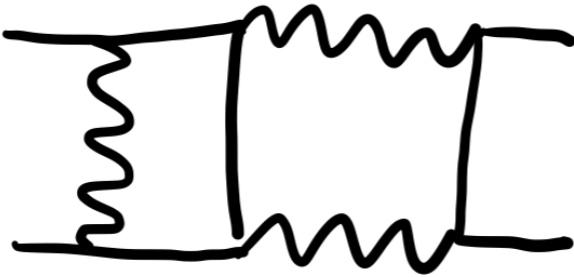
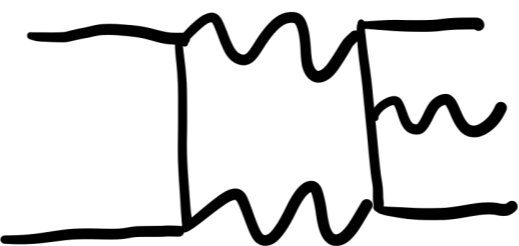
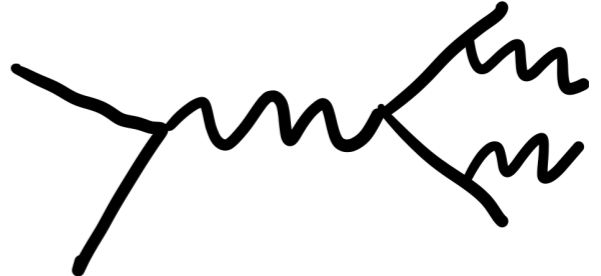
NEXT-TO-  
NEXT-TO-  
LEADING  
ORDER (NNLO)



# PRECISION TESTS OF THE STANDARD MODEL

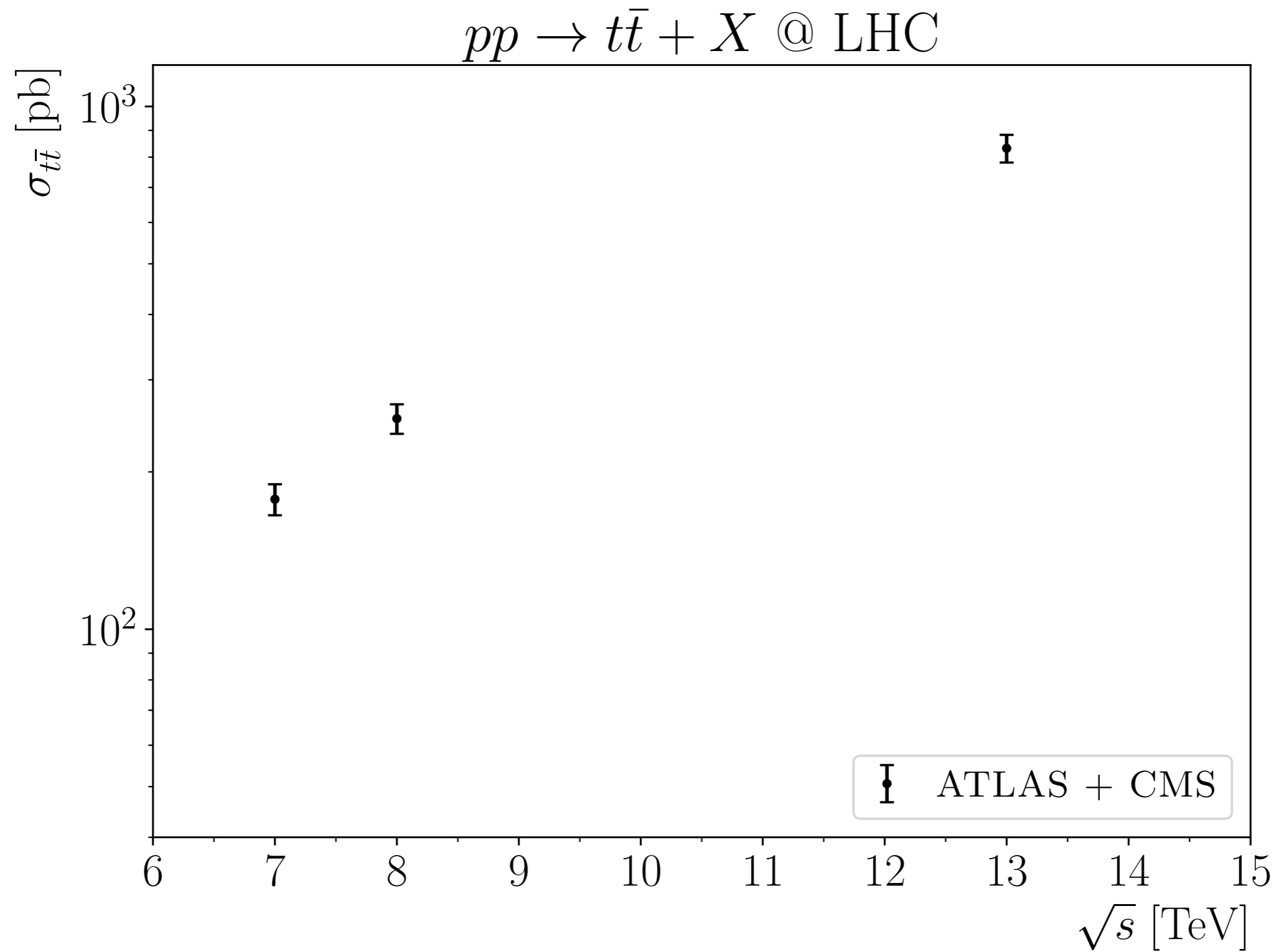
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- High precision in the theoretical prediction requires the computation of **higher order corrections**.

<b>LEADING ORDER (LO)</b>			
<b>NEXT-TO LEADING ORDER (NLO)</b>			
<b>NEXT-TO- NEXT-TO- LEADING ORDER (NNLO)</b>			

# THE IMPORTANCE OF PRECISION

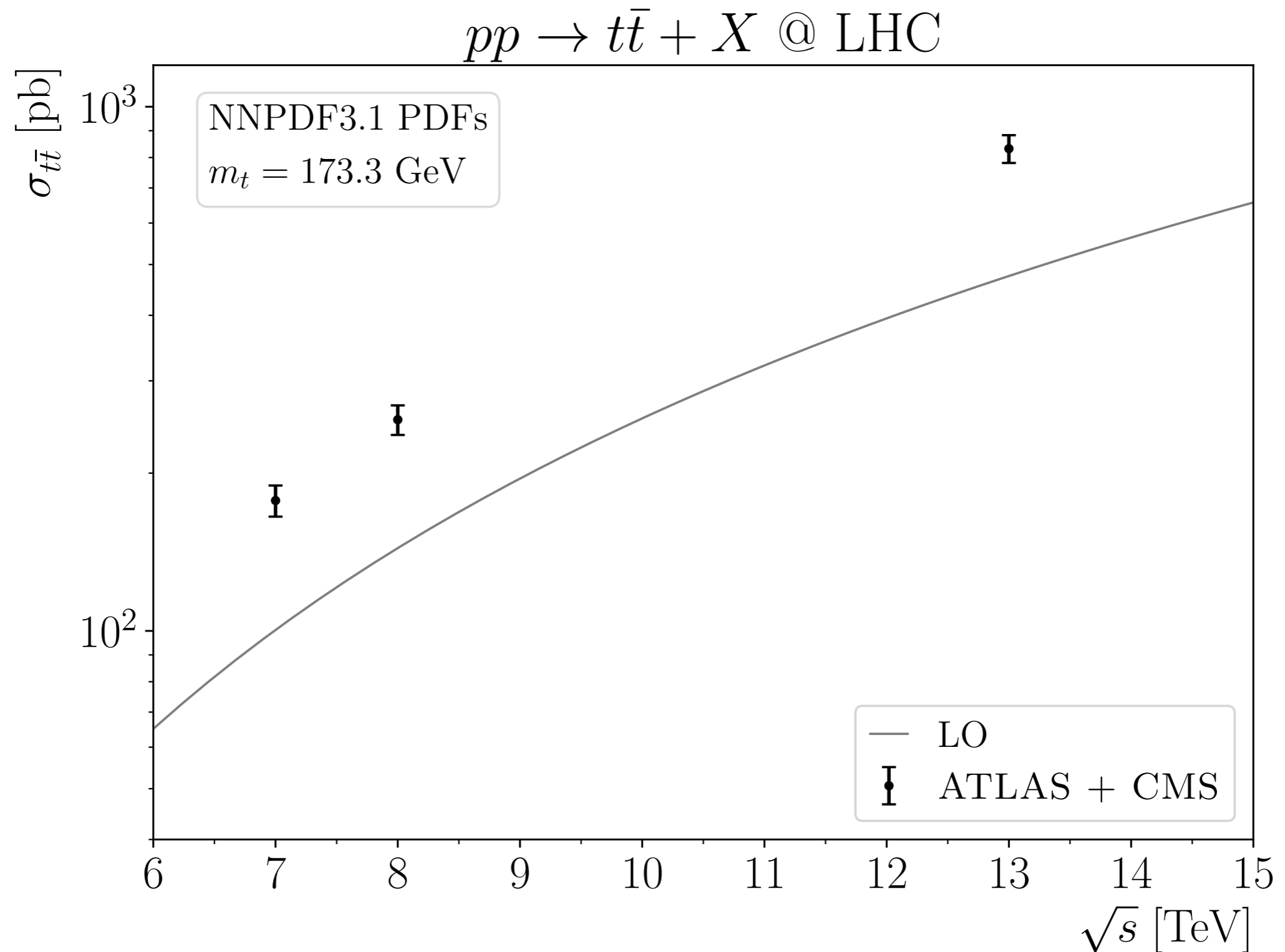
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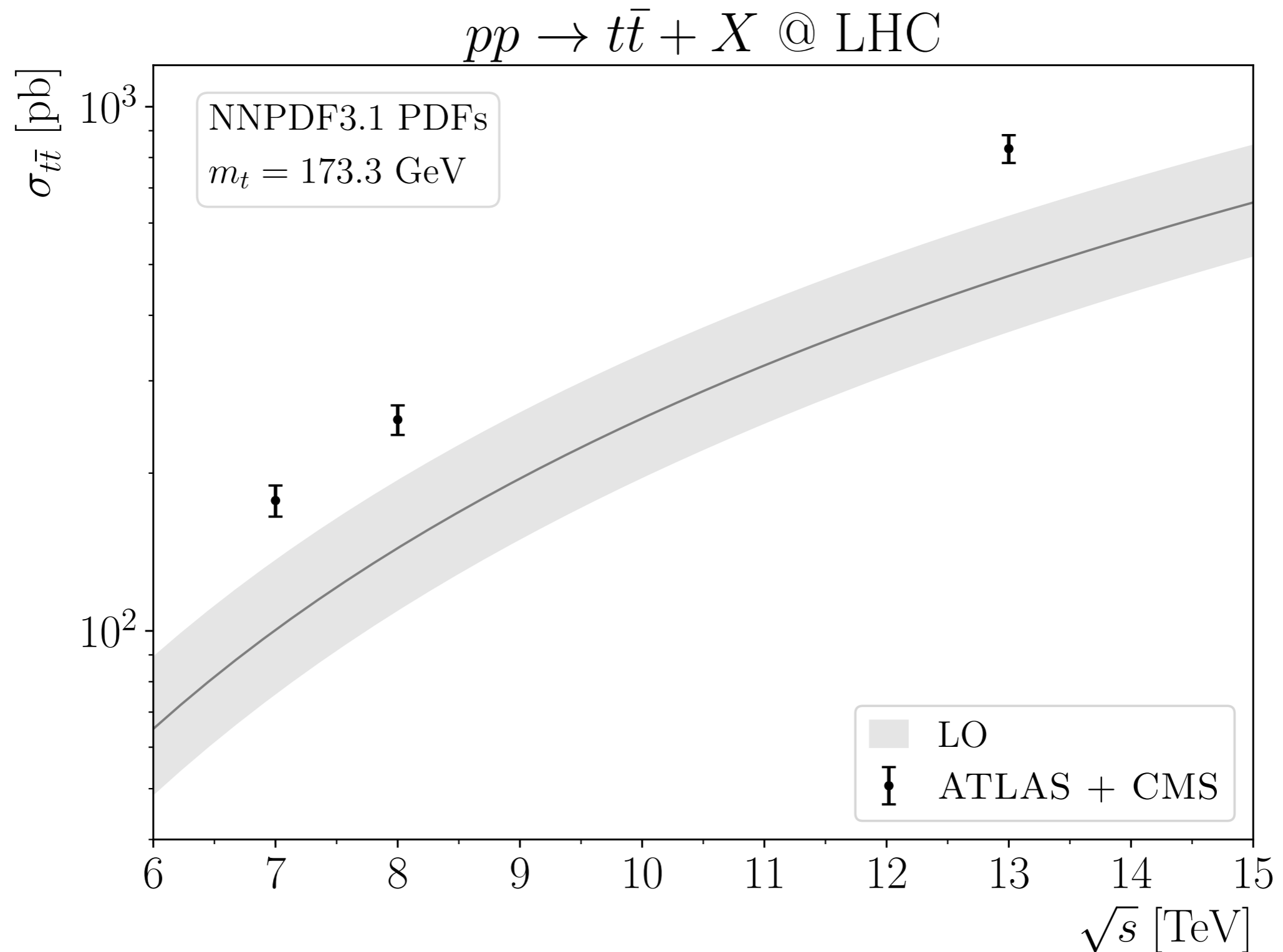
# THE IMPORTANCE OF PRECISION

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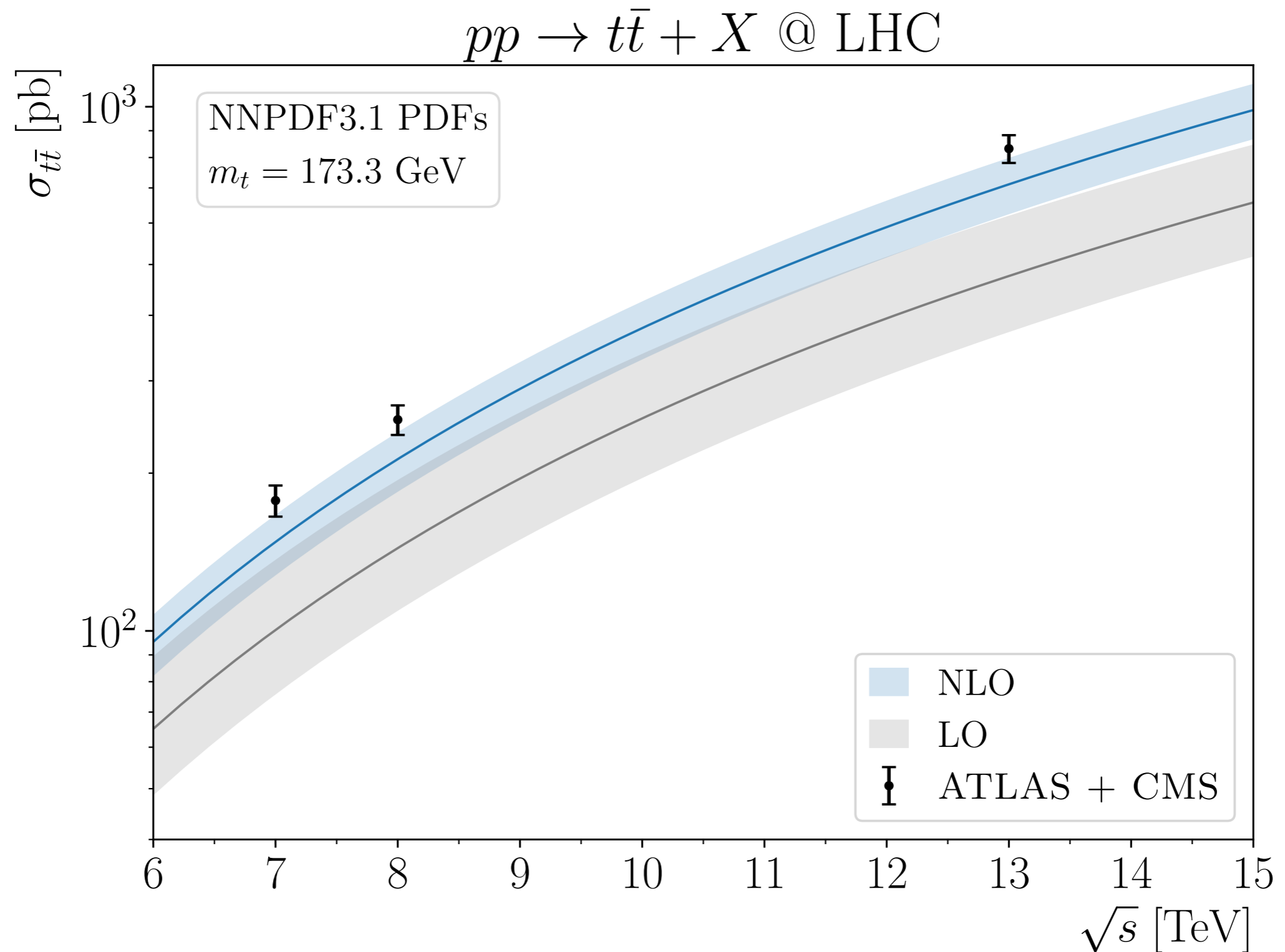


# THE IMPORTANCE OF PRECISION

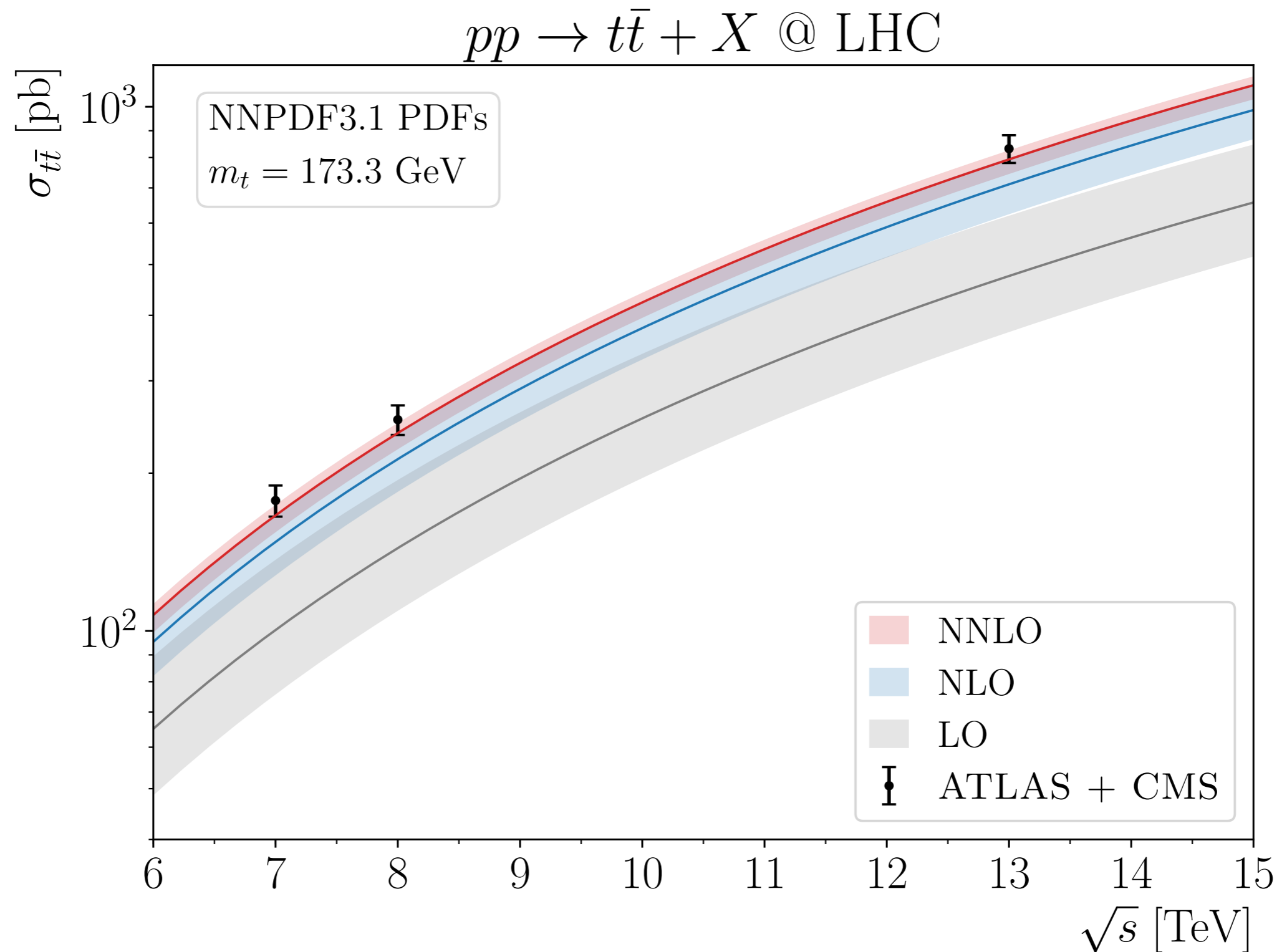
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# THE IMPORTANCE OF PRECISION



# THE IMPORTANCE OF PRECISION



# THE MATRIX FRAMEWORK

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[M. Grazzini, S. Kallweit,  
M. Wiesemann: 1711.06631]

## MUNICH

MUlti-ChaNNel Integrator at Swiss (CH) precision

### OPENLOOPS

(Collier, CutTools...)

### TWO-LOOP AMPLITUDES

(VVamp, GiNaC, tdhpl...)

$q_T$  subtraction



## MATRIX

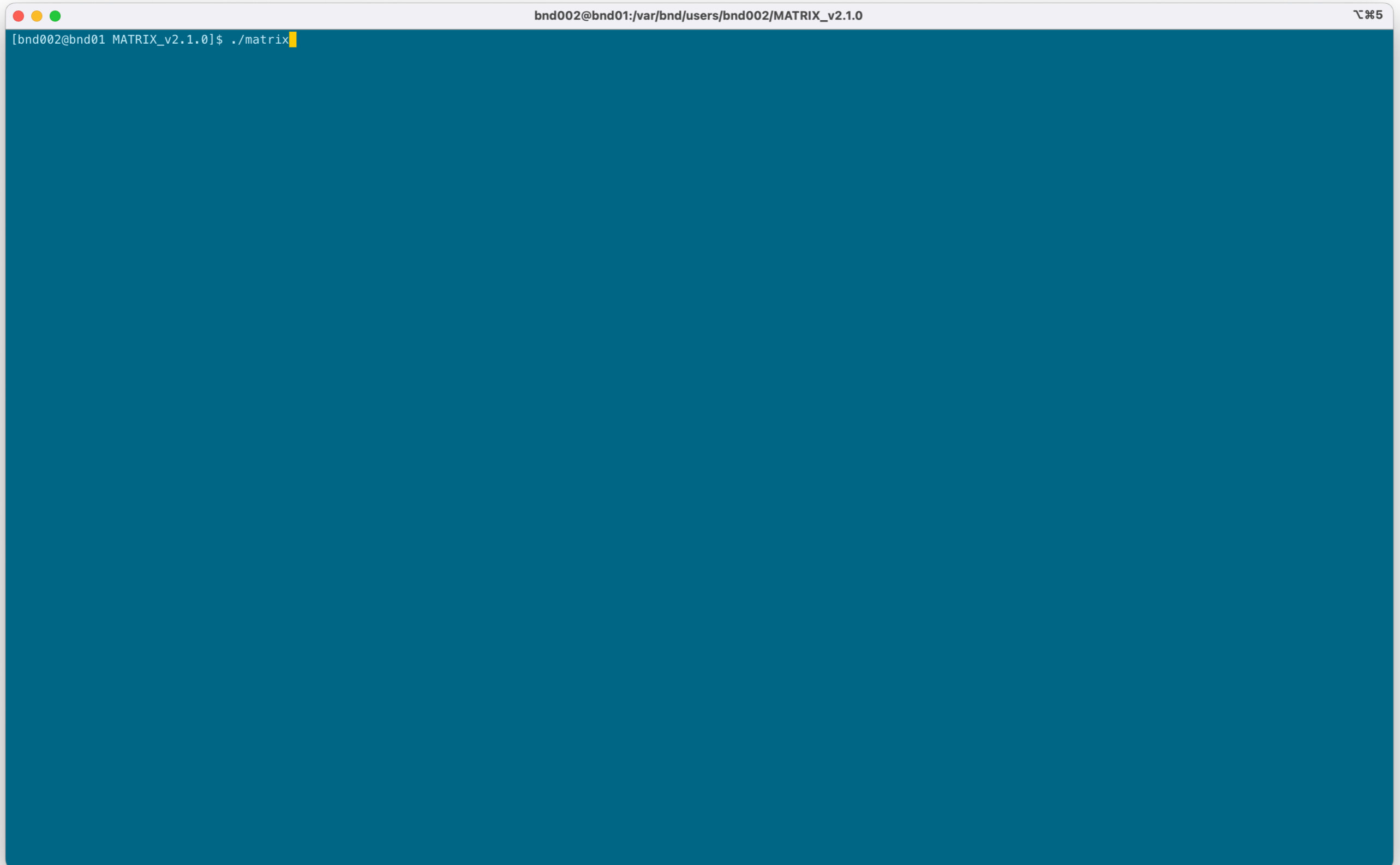
Munich Automates  $q_T$  subtraction

and Resummation to Integrate X-sections

Code publicly available at <https://matrix.hepforge.org>

# THE MATRIX FRAMEWORK

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A terminal window with a white title bar and a blue background. The title bar contains three colored window control buttons (red, yellow, green) on the left, the text `bnd002@bnd01:/var/bnd/users/bnd002/MATRIX_v2.1.0` in the center, and a keyboard shortcut icon on the right. The terminal content shows a shell prompt `[bnd002@bnd01 MATRIX_v2.1.0]$` followed by the command `./matrix` and a yellow cursor.

```
[bnd002@bnd01 MATRIX_v2.1.0]$ ./matrix
```







# THE MATRIX FRAMEWORK

bnd002@bnd01:/var/bnd/users/bnd002/MATRIX\_v2.1.0

⌘5

```
Munich -- the Multi-channel Integrator at swiss (CH) precision --  
Automates qT-subtraction and Resummation to Integrate X-sections
```



```
M. Grazzini (grazzini@physik.uzh.ch)  
S. Kallweit (stefan.kallweit@cern.ch)  
M. Wiesemann (maris.wiesemann@cern.ch)
```

```
MATRIX is based on a number of different computations and tools  
from various people and groups. Please acknowledge their efforts  
by citing the references in CITATIONS.bib created with every run.
```

```
<<MATRIX-MAKE>> This is the MATRIX process compilation.  
<<MATRIX-READ>> Type process_id to be compiled and created. Type "list" to show  
available processes. Try pressing TAB for auto-completion. Type  
"exit" or "quit" to stop.
```

```
|=====>> list
```

process_id	process	description
p-ph21	p p --> H	on-shell Higgs production (NNLO)
ppz01	p p --> Z	on-shell Z production (NNLO,NLO EW)
ppw01	p p --> W-	on-shell W- production with CKM (NNLO)
ppwx01	p p --> W+	on-shell W+ production with CKM (NNLO)
p-peex02	p p --> e- e+	Z production with decay (NNLO,NLO EW)
ppnenex02	p p --> nu_e- nu_e+	Z production with decay (NNLO,NLO EW)
ppnex02	p p --> e- nu_e+	W- production with decay and CKM (NNLO,NLO EW)
ppexne02	p p --> e+ nu_e-	W+ production with decay and CKM (NNLO,NLO EW)
ppaa02	p p --> gamma gamma	gamma gamma production (NNLO)
p-peexa03	p p --> e- e+ gamma	Z gamma production with decay (NNLO)
ppnenexa03	p p --> nu_e- nu_e+ gamma	Z gamma production with decay (NNLO)
ppnexa03	p p --> e- nu_e+ gamma	W- gamma production with decay (NNLO)
ppexnea03	p p --> e+ nu_e- gamma	W+ gamma production with decay (NNLO)
ppzz02	p p --> Z Z	on-shell ZZ production (NNLO)
ppwxw02	p p --> W+ W-	on-shell WW production (NNLO)
ppemexmx04	p p --> e- mu- e+ mu+	ZZ production with decay (NNLO,NLO gg,NLO EW)
p-peeexex04	p p --> e- e- e+ e+	ZZ production with decay (NNLO,NLO gg,NLO EW)
p-peexnmx04	p p --> e- e+ nu_mu- nu_mu+	ZZ production with decay (NNLO,NLO gg,NLO EW)
ppemxnmex04	p p --> e- mu+ nu_mu- nu_e+	WW production with decay (NNLO,NLO gg,NLO EW)
p-peexnmx04	p p --> e- e+ nu_e- nu_e+	ZZ/WW production with decay (NNLO,NLO gg,NLO EW)
ppemexnm04	p p --> e- mu- e+ nu_mu+	W-Z production with decay (NNLO,NLO EW)
p-peeexnex04	p p --> e- e- e+ nu_e+	W-Z production with decay (NNLO,NLO EW)
p-peexmxnm04	p p --> e- e+ mu+ nu_mu-	W+Z production with decay (NNLO,NLO EW)
p-peexexne04	p p --> e- e+ e+ nu_e-	W+Z production with decay (NNLO,NLO EW)
pp-ttx20	p p --> top anti-top	on-shell top-pair production (NNLO)
ppaaa03	p p --> gamma gamma gamma	gamma gamma gamma production (NNLO)

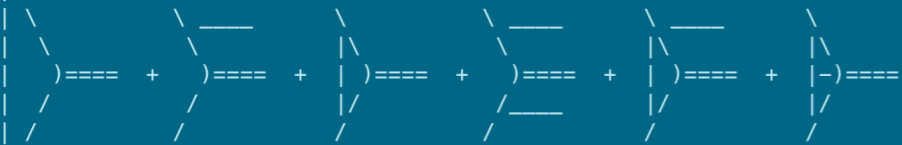
```
|=====>>
```

# THE MATRIX FRAMEWORK

bnd002@bnd01:/var/bnd/users/bnd002/MATRIX\_v2.1.0

⌘5

```
Munich -- the MULTI-chaNnel Integrator at swiss (CH) precision --  
Automates qT-subtraction and Resummation to Integrate X-sections
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```
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ppwx01	p p --> W^+	on-shell W+ production with CKM (NNLO)
ppeex02	p p --> e^- e^+	Z production with decay (NNLO,NLO EW)
ppnenex02	p p --> v_e^- v_e^+	Z production with decay (NNLO,NLO EW)
ppnex02	p p --> e^- v_e^+	W- production with decay and CKM (NNLO,NLO EW)
ppexne02	p p --> e^+ v_e^-	W+ production with decay and CKM (NNLO,NLO EW)
ppaa02	p p --> gamma gamma	gamma gamma production (NNLO)
ppeexa03	p p --> e^- e^+ gamma	Z gamma production with decay (NNLO)
ppnenexa03	p p --> v_e^- v_e^+ gamma	Z gamma production with decay (NNLO)
ppnexa03	p p --> e^- v_e^+ gamma	W- gamma production with decay (NNLO)
ppexnea03	p p --> e^+ v_e^- gamma	W+ gamma production with decay (NNLO)
ppzz02	p p --> Z Z	on-shell ZZ production (NNLO)
ppwxw02	p p --> W^+ W^-	on-shell WW production (NNLO)
ppemxmx04	p p --> e^- mu^- e^+ mu^+	ZZ production with decay (NNLO,NLO gg,NLO EW)
ppeeexex04	p p --> e^- e^- e^+ e^+	ZZ production with decay (NNLO,NLO gg,NLO EW)
ppeexnmnx04	p p --> e^- e^+ v_mu^- v_mu^+	ZZ production with decay (NNLO,NLO gg,NLO EW)
ppemxnmnx04	p p --> e^- mu^+ v_mu^- v_e^+	WW production with decay (NNLO,NLO gg,NLO EW)
ppeexnenex04	p p --> e^- e^+ v_e^- v_e^+	ZZ/WW production with decay (NNLO,NLO gg,NLO EW)
ppemxnmx04	p p --> e^- mu^- e^+ v_mu^+	W-Z production with decay (NNLO,NLO EW)
ppeeexnex04	p p --> e^- e^- e^+ v_e^+	W-Z production with decay (NNLO,NLO EW)
ppexmxnm04	p p --> e^- e^+ mu^+ v_mu^-	W+Z production with decay (NNLO,NLO EW)
ppeexxne04	p p --> e^- e^+ e^+ v_e^-	W+Z production with decay (NNLO,NLO EW)
ppttx20	p p --> top anti-top	on-shell top-pair production (NNLO)
ppaaa03	p p --> gamma gamma gamma	gamma gamma gamma production (NNLO)

# THE TOP QUARK

The **top quark** is the **heaviest** particle in the Standard Model:  $m_t \approx 173 \text{ GeV}$ .


1																	18		
1	2												13	14	15	16	17	18	
1	2												5	6	7	8	9	10	
2	4												13	14	15	16	17	18	
3	12												13	14	15	16	17	18	
4	20		3	4	5	6	7	8	9	10	11	12	31	32	33	34	35	36	
5	38		39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	
6	56		57-71		72	73	74	75	76	77	78	79	80	81	82	83	84	85	86
7	88		89-103		104	105	106	107	108	109	110	111	112	113	114	115	116	117	118

Number  
Symbol  
Name  
Atomic Mass

57 <b>La</b> Lanthanum 138.905	58 <b>Ce</b> Cerium 140.116	59 <b>Pr</b> Praseodymium 140.908	60 <b>Nd</b> Neodymium 144.243	61 <b>Pm</b> Promethium 144.913	62 <b>Sm</b> Samarium 150.36	63 <b>Eu</b> Europium 151.964	64 <b>Gd</b> Gadolinium 157.25	65 <b>Tb</b> Terbium 158.925	66 <b>Dy</b> Dysprosium 162.500	67 <b>Ho</b> Holmium 164.930	68 <b>Er</b> Erbium 167.259	69 <b>Tm</b> Thulium 168.934	70 <b>Yb</b> Ytterbium 173.055	71 <b>Lu</b> Lutetium 174.967
89 <b>Ac</b> Actinium 227.028	90 <b>Th</b> Thorium 232.038	91 <b>Pa</b> Protactinium 231.036	92 <b>U</b> Uranium 238.029	93 <b>Np</b> Neptunium 237.048	94 <b>Pu</b> Plutonium 244.064	95 <b>Am</b> Americium 243.061	96 <b>Cm</b> Curium 247.070	97 <b>Bk</b> Berkelium 247.070	98 <b>Cf</b> Californium 251.080	99 <b>Es</b> Einsteinium [254]	100 <b>Fm</b> Fermium 257.095	101 <b>Md</b> Mendelevium 258.1	102 <b>No</b> Nobelium 259.101	103 <b>Lr</b> Lawrencium [262]


# THE TOP QUARK

The **top quark** is the **heaviest** particle in the Standard Model:  $m_t \simeq 173 \text{ GeV}$ .

1	1	2											13	14	15	16	17	18	
1	<b>1</b> H Hydrogen 1.008																		<b>2</b> He Helium 4.003
2	<b>3</b> Li Lithium 6.941	<b>4</b> Be Beryllium 9.012											<b>5</b> B Boron 10.811	<b>6</b> C Carbon 12.011	<b>7</b> N Nitrogen 14.007	<b>8</b> O Oxygen 15.999	<b>9</b> F Fluorine 18.998	<b>10</b> Ne Neon 20.180	
3	<b>11</b> Na Sodium 22.990	<b>12</b> Mg Magnesium 24.305											<b>13</b> Al Aluminum 26.982	<b>14</b> Si Silicon 28.086	<b>15</b> P Phosphorus 30.974	<b>16</b> S Sulfur 32.066	<b>17</b> Cl Chlorine 35.453	<b>18</b> Ar Argon 39.948	
4	<b>19</b> K Potassium 39.098	<b>20</b> Ca Calcium 40.078	<b>21</b> Sc Scandium 44.956	<b>22</b> Ti Titanium 47.867	<b>23</b> V Vanadium 50.942	<b>24</b> Cr Chromium 51.996	<b>25</b> Mn Manganese 54.938	<b>26</b> Fe Iron 55.845	<b>27</b> Co Cobalt 58.933	<b>28</b> Ni Nickel 58.693	<b>29</b> Cu Copper 63.546	<b>30</b> Zn Zinc 65.38	<b>31</b> Ga Gallium 69.723	<b>32</b> Ge Germanium 72.631	<b>33</b> As Arsenic 74.922	<b>34</b> Se Selenium 78.971	<b>35</b> Br Bromine 79.904	<b>36</b> Kr Krypton 83.798	
5	<b>37</b> Rb Rubidium 85.468	<b>38</b> Sr Strontium 87.62	<b>39</b> Y Yttrium 88.906	<b>40</b> Zr Zirconium 91.224	<b>41</b> Nb Niobium 92.906	<b>42</b> Mo Molybdenum 95.95	<b>43</b> Tc Technetium 98.907	<b>44</b> Ru Ruthenium 101.07	<b>45</b> Rh Rhodium 102.906	<b>46</b> Pd Palladium 106.42	<b>47</b> Ag Silver 107.868	<b>48</b> Cd Cadmium 112.411	<b>49</b> In Indium 114.818	<b>50</b> Sn Tin 118.710	<b>51</b> Sb Antimony 121.757	<b>52</b> Te Tellurium 127.6	<b>53</b> I Iodine 126.904	<b>54</b> Xe Xenon 131.293	
6	<b>55</b> Cs Cesium 132.905	<b>56</b> Ba Barium 137.328	57-71 Lanthanoids	<b>72</b> Hf Hafnium 178.49	<b>73</b> Ta Tantalum 180.948		<b>75</b> Re Rhenium 186.207	<b>76</b> Os Osmium 190.23	<b>77</b> Ir Iridium 192.217	<b>78</b> Pt Platinum 195.085	<b>79</b> Au Gold 196.967	<b>80</b> Hg Mercury 200.59	<b>81</b> Tl Thallium 204.38	<b>82</b> Pb Lead 207.2	<b>83</b> Bi Bismuth 208.98	<b>84</b> Po Polonium [209]	<b>85</b> At Astatine 209.987	<b>86</b> Rn Radon 222.018	
7	<b>87</b> Fr Francium 223.020	<b>88</b> Ra Radium 226.025	89-103 Actinoids	<b>104</b> Rf Rutherfordium [261]	<b>105</b> Db Dubnium [262]	<b>106</b> Sg Seaborgium [266]	<b>107</b> Bh Bohrium [264]	<b>108</b> Hs Hassium [269]	<b>109</b> Mt Meitnerium [278]	<b>110</b> Ds Darmstadtium [281]	<b>111</b> Rg Roentgenium [282]	<b>112</b> Cn Copernicium [285]	<b>113</b> Nh Nihonium [284]	<b>114</b> Fl Flerovium [287]	<b>115</b> Mc Moscovium [288]	<b>116</b> Lv Livermorium [293]	<b>117</b> Ts Tennessine [294]	<b>118</b> Og Oganesson [294]	

Number  
**Symbol**  
Name  
Atomic Mass


TOP QUARK



t

Discovered at Fermilab in 1995, the **TOP QUARK** is as short-lived as it is massive. Weighing in at a hefty 175 GeV, its lifetime, a mere  $10^{-24}$  second, is the briefest of the six quarks. Top Quarks are an enigmatic particle whose personal life is sought after by thousands of physicists.

<b>57</b> La Lanthanum 138.905	<b>58</b> Ce Cerium 140.116	<b>59</b> Pr Praseodymium 140.908	<b>60</b> Nd Neodymium 144.243	<b>61</b> Pm Promethium 144.913	<b>62</b> Sm Samarium 150.36	<b>63</b> Eu Europium 151.964	<b>64</b> Gd Gadolinium 157.25
<b>89</b> Ac Actinium 227.028	<b>90</b> Th Thorium 232.038	<b>91</b> Pa Protactinium 231.036	<b>92</b> U Uranium 238.029	<b>93</b> Np Neptunium 237.048	<b>94</b> Pu Plutonium 244.064	<b>95</b> Am Americium 243.061	<b>96</b> Cm Curium 247



<b>70</b> Yb Ytterbium 173.055	<b>71</b> Lu Lutetium 174.967
<b>102</b> No Nobelium 259.101	<b>103</b> Lr Lawrencium [262]

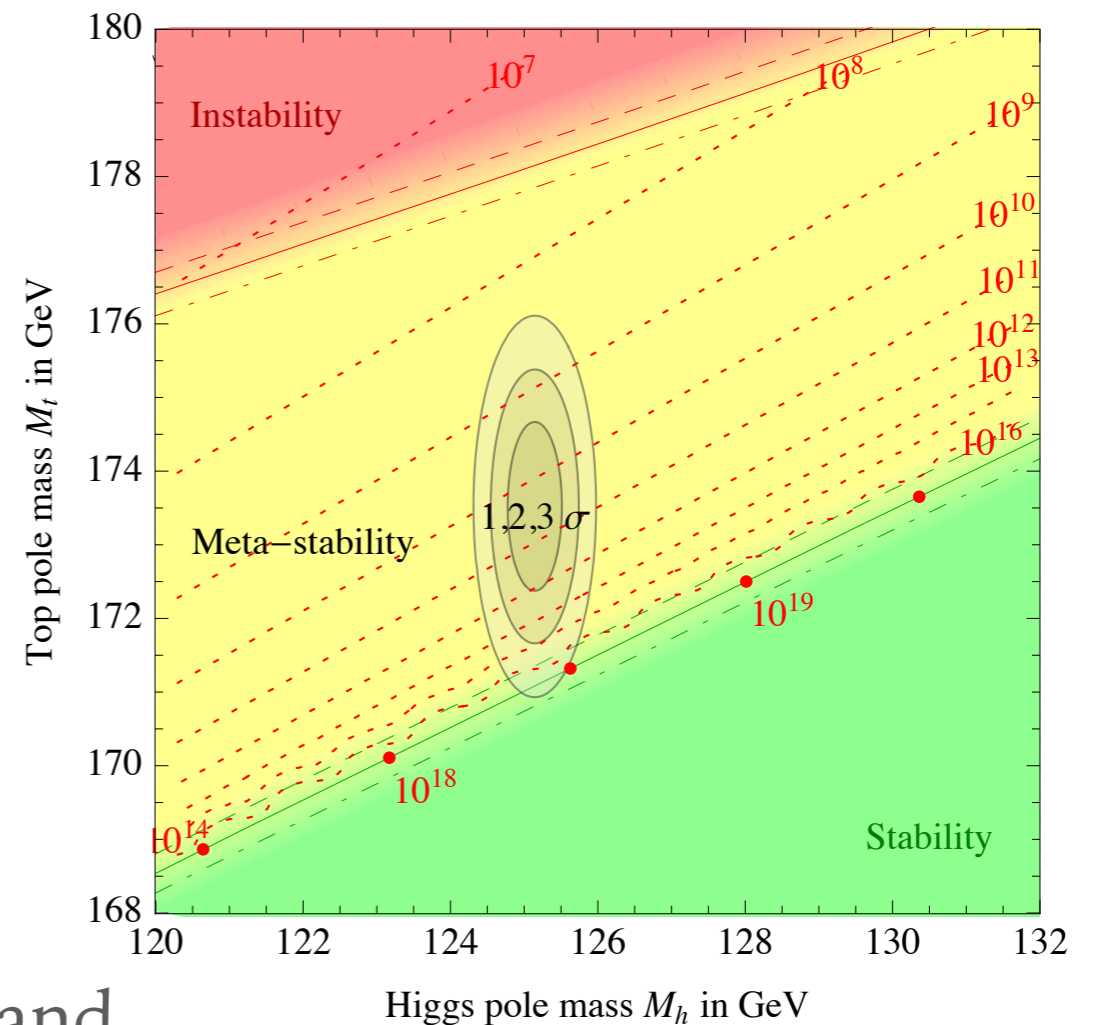
©2018 sciencenotes.org

7

# THE TOP QUARK

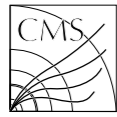
The Top Quark plays a major role both in Standard Model studies and Beyond the Standards Model searches!

- Has a strong coupling with the **Higgs boson**;
- The top mass is a **fundamental parameter** of the Standard Model;
- The value of the top mass plays a key role in **vacuum stability**;
- The top mass is a **standard candle** at LHC;
- possible window on **New Physics**;
- **Important background** both for SM and BSM studies.



# EXPERIMENTAL MEASUREMENTS

EUROPEAN ORGANIZATION FOR NUCLEAR RESEARCH (CERN)



CMS-TOP-17-002

CERN-EP-2018-039  
2018/06/19

Measurement of differential cross sections for the production of top quark pairs and of additional jets in lepton+jets events from pp collisions at  $\sqrt{s} = 13$  TeV

The CMS Collaboration\*

## Abstract

Differential and double-differential cross sections for the production of top quark pairs in proton-proton collisions at  $\sqrt{s} = 13$  TeV are measured as a function of kinematic variables of the top quarks and the top quark-antiquark ( $t\bar{t}$ ) system. In addition, kinematic variables and multiplicities of jets associated with the  $t\bar{t}$  production are measured. This analysis is based on data collected by the CMS experiment at the LHC in 2016 corresponding to an integrated luminosity of  $35.8 \text{ fb}^{-1}$ . The measurements are performed in the lepton+jets decay channels with a single muon or electron and jets in the final state. The differential cross sections are presented at the particle level, within a phase space close to the experimental acceptance, and at the parton level in the full phase space. The results are compared to several standard model predictions that use different methods and approximations. The kinematic variables of the top quarks and the  $t\bar{t}$  system are reasonably described in general, though none predict all the measured distributions. In particular, the transverse momentum distribution of the top quarks is more steeply falling than predicted. The kinematic distributions and multiplicities of jets are adequately modeled by certain combinations of next-to-leading-order calculations and parton shower models.

Published in *Physical Review D* as [doi:10.1103/PhysRevD.97.112003](https://doi.org/10.1103/PhysRevD.97.112003).

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\*See Appendix E for the list of collaboration members

25

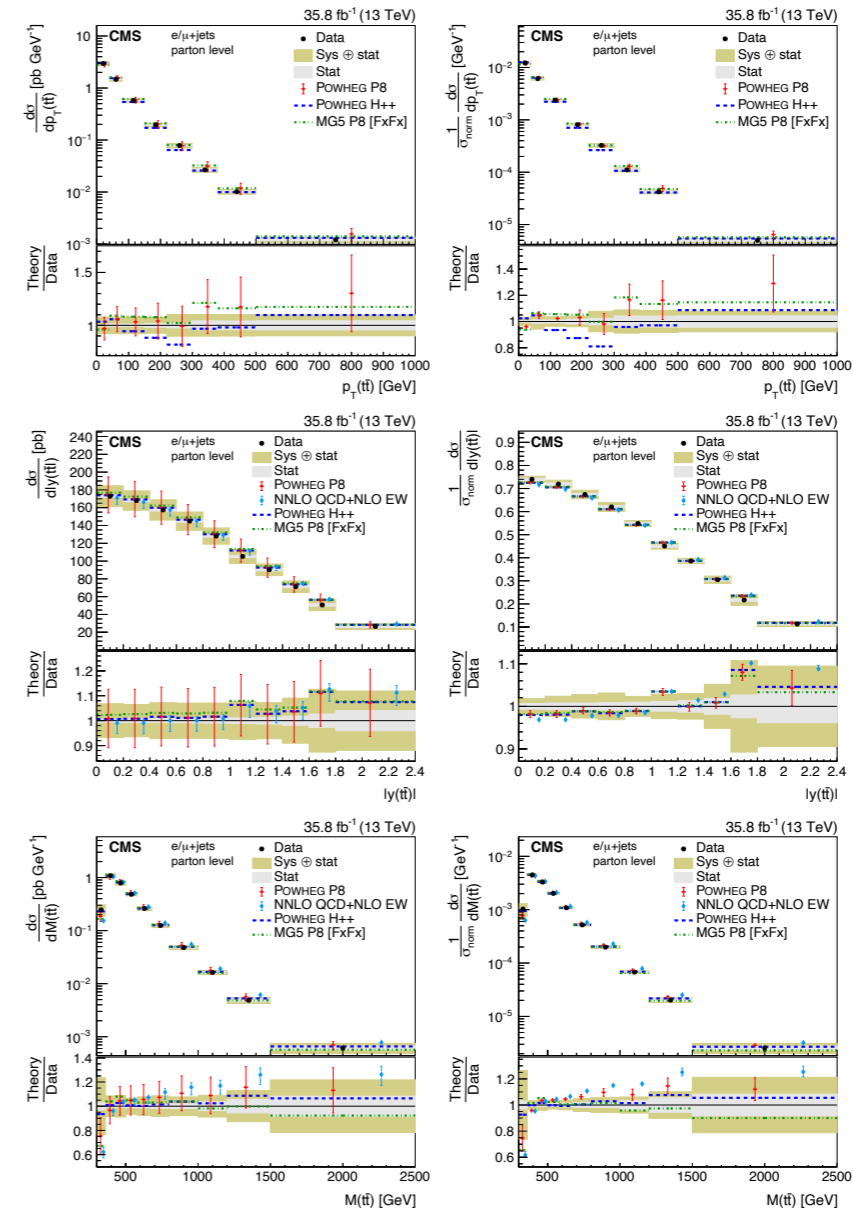


Figure 16: Absolute (left) and normalized (right) differential cross sections at the parton level as a function of  $p_T(t\bar{t})$  (upper),  $|y(t\bar{t})|$  (middle), and  $M(t\bar{t})$  (lower). The data are shown as points with light (dark) bands indicating the statistical (statistical and systematic) uncertainties. The cross sections are compared to the predictions of POWHEG combined with PYTHIA8 (P8) or HERWIG++ (H++), the multiparton simulation MG5\_aMC@NLO (MG5)+PYTHIA8 FxFx, and the NNLO QCD+NLO EW calculations. The ratios of the various predictions to the measured cross sections are shown at the bottom of each panel.

arXiv:1803.08856v2 [hep-ex] 18 Jun 2018

# THE PROJECT

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The CMS collaboration measured differential distributions for top pair production in the lepton+jet channel (Phys. Rev. D,97(11):112003, 2018), presenting parton level results.

- **Use MATRIX to compute NNLO theoretical predictions for the invariant mass of the  $t\bar{t}$  pair,  $m_{t\bar{t}}$ , and the transverse momentum of the hadronically decaying top,  $p_{T,t_{had}}$ .** Fix the value of the top mass to  $m_t = 173.3$  GeV and use the NNPDF31 set of parton distribution functions with  $\alpha_s(m_Z) = 0.118$ . Consider different choices for the central value  $\mu_0$  of the renormalization and factorization scale:  $H_T/2$ ,  $H_T/4$ ,  $m_{t\bar{t}}/2$ ,  $m_{T,t}$ ,  $m_{T,\bar{t}}$ , where  $m_{T,t(\bar{t})}$  is the transverse mass of the (anti-)top quark, and  $H_T$  is defined as  $H_T = m_{T,t} + m_{T,\bar{t}}$ .
- **Plot the differential distributions** obtained for different central scale choices. What do you observe? Which ones exhibit a faster perturbative convergence? Which ones provide a more reliable estimate of the theoretical uncertainties?
- **Compare the theoretical predictions with experimental data.** How does the central scale choice affect the comparison? Do you observe agreement between theory and experimental measurements? If not, can you think about possible justifications?

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